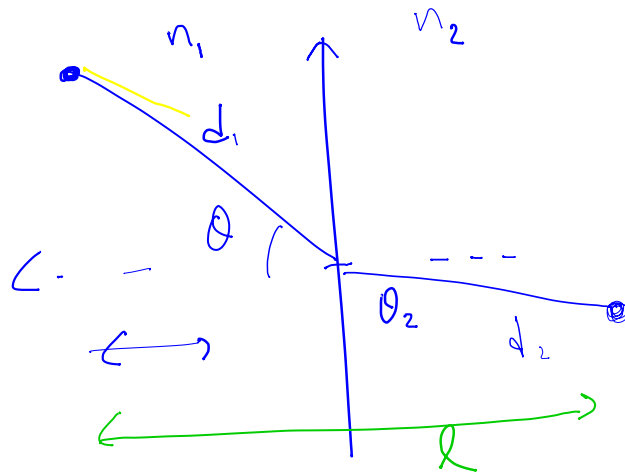


91 Snell's law $n_1 \sin \theta_1 = n_2 \sin \theta_2$

Fermat's principle: ray of light chooses path that minimizes time to travel



total time

$$t = \frac{d_1}{v_1} + \frac{d_2}{v_2}$$

since $n = \frac{c}{v}$

$$= \frac{d_1}{\frac{c}{n_1}} + \frac{d_2}{\frac{c}{n_2}}$$

$$= \frac{\sqrt{h^2 + x^2}}{c n_1} + \frac{\sqrt{h^2 + (l-x)^2}}{c n_2}$$

$\frac{dt}{dx} = 0$ would give us the extreme (hopefully minimum)

$$\Rightarrow n_1 \frac{x}{\sqrt{h^2 + x^2}} = n_2 \frac{(-1)}{\sqrt{h^2 + (l-x)^2}}$$

$\underbrace{\hspace{10em}}_{\sin \theta_1} \qquad \underbrace{\hspace{10em}}_{\sin \theta_2}$

92 a) Fresnel's eq. $L_2 \left[\begin{array}{c} \frac{2 \sin \theta_2 \cos \theta_0}{\sin(\theta_2 - \theta_0)} \vec{e}_0 \\ \frac{\sin(\theta_2 - \theta_0)}{\sin(\theta_2 + \theta_0)} L_0 \end{array} \right]$ } perp to plane of incidence

$T = \frac{\tan(\theta_0 - \theta_2)}{\tan(\theta_0 + \theta_2)} T_0$ } parallel to plane of incidence

$t_2 = \frac{2 \cos \theta_0 \sin \theta_2}{\sin(\theta_0 - \theta_2) \cos(\theta_0 + \theta_2)} \vec{e}_0$

$\vec{p} \cdot \vec{L} = \vec{L} \cdot \vec{p} = \sqrt{\frac{\epsilon}{\mu}} \hat{n} \cdot \vec{L} = \sqrt{\frac{\epsilon}{\mu}} L^2 \hat{n} = \frac{n}{\mu c} L^2 \hat{n}$
 as $n = \sqrt{\mu \epsilon}$

Reflectivity $R = \frac{L^2}{L_0^2}$

$R = \frac{\tan^2(\theta_0 - \theta_2)}{\tan^2(\theta_0 + \theta_2)}$ $R = \frac{\sin^2(\theta_2 - \theta_0)}{\sin^2(\theta_2 + \theta_0)}$

$\frac{n_2}{n_0} \frac{L_2^2}{L_0^2}$

$\frac{n_2}{n_0} \frac{4 \sin^2 \theta_2 \cos^2 \theta_0}{\sin^2(\theta_2 - \theta_0)}$

can use sine rule to simplify...

$$\frac{n_2 \cos^2 \theta_0 \sin^2 \theta_2}{n \sin^2(\theta_0 - \theta_2) \cos^2(\theta_0 - \theta_2)}$$

b) $R = \frac{\sin^2(\theta_2 - \theta_0)}{\sin^2(\theta_2 + \theta_0)}$

since this is reflected
we know that $\theta_0 - \theta_2$
we also know (Snell's)

$$\frac{\sin \theta_0}{\sin \theta_2} = \frac{n_2}{n}$$

when $\theta > 0$ $\theta = \theta_2$ $\frac{n_2}{n}$

$$R \approx \frac{\left\{ \sin \left[\theta_2 \left(\frac{n_2}{n} \right) \right] \right\}^2}{\left\{ \sin \left[\theta_2 \left(\frac{n_2}{n} \right) \right] \right\}^2}$$

$$\approx \frac{\left(\frac{n_2}{n} \right)^2}{\left(\frac{n_2}{n} \right)^2} = \frac{(n - n_2)^2}{(n + n_2)^2}$$

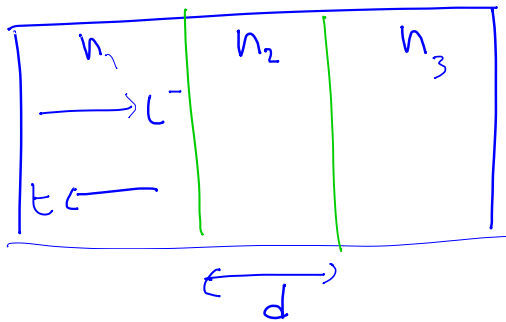
- 0.09 when $n = n_2 - 5$

c) From book for $\theta_{\text{brester}} = \frac{n_2}{n}$

) $\theta_{\text{brester}} = \sin^{-1} \left(\frac{n_2}{n} \right) = 56.3^\circ$

d) $\theta_{\text{crit}} = \sin^{-1} \left(\frac{n_2}{n} \right) = 41.8^\circ$

9.3 /



From before we know that
(prob 9.2b)

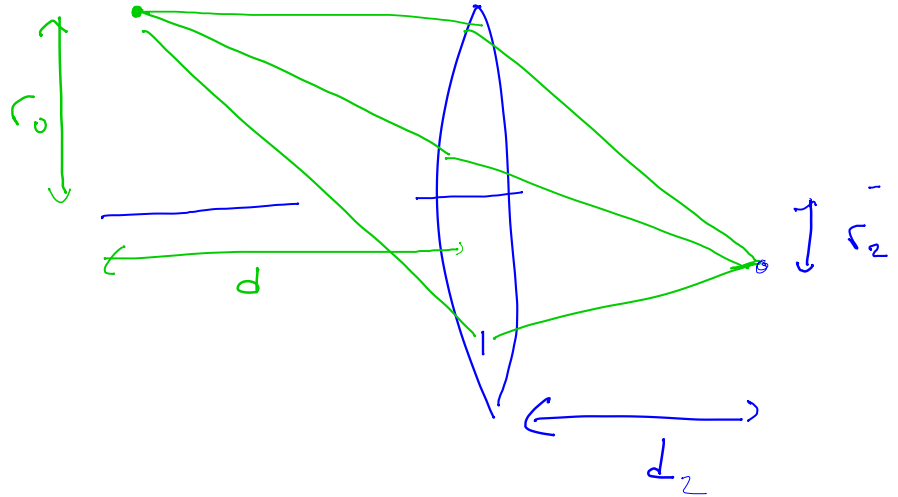
$$R = \frac{\sin(\theta_2 - \theta_0)}{\sin(\theta_2 + \theta_0)}$$

$$\approx \frac{n_2/n}{n/n_2} \quad ??$$

94/

ray matrix for lens

$$s \begin{bmatrix} 1 & 0 \\ 1/s & 1 \end{bmatrix}$$



from eq. 9.37

$$\begin{bmatrix} 1 & d_2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 1/s & 1 \end{bmatrix} \begin{bmatrix} 1 & d_1 \\ 0 & 1 \end{bmatrix}$$

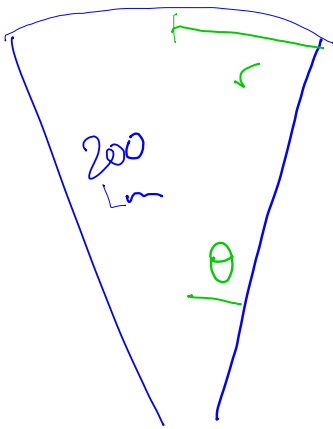
$$\begin{bmatrix} -d_2/s & d & d_2(d_1/s) \\ 1/s & d/s & 1 \end{bmatrix} \quad \bar{\wedge}$$

$$9.5/a) \theta = \frac{\lambda}{nw} = \frac{790 \text{ nm}}{1 \cdot 0.6 \text{ m}} = 0.25 \text{ rad}$$

$n = \text{air}$

b) $\lambda = \pi n w \theta$
 $78 \text{ nm} \quad (\text{rays?})$

c) Diffraction angle $\theta = \frac{600 \text{ nm}}{r \cdot 0.2} = 9 \text{ } 10^5 \text{ rad.}$
 $\underbrace{\hspace{2cm}}_{0.2 \text{ m}}$



$$\tan \theta = \frac{r}{200 \text{ m}}$$

$$\rightarrow r \approx 38 \text{ m}$$

