# Flexure based Machine Design

"How to make almost anything" Nov. 6 2006 Manu Prakash

### Serial and Parallel

- Serial : actuators mounted on top of each other
  - Bulky for high DOF, slow response
- Parallel : each actuator mounted on ground base
  - Close chain parallel design, increased crosssensitivity



### Flexures

- Overcome backlash with repeatable joints
- Ease of fabrication
- Very few joints
- Sub-micron accuracy achieved easily
- Limited range of motion
- Careful material selection

### Flexures in biology

### Fish fin and body dynamics -



### Energy storage in Venus fly trap



### Drag reduction in leaves aquaplaning





2D

3D

### Flexure analysis

#### Simple beam flexure



$$\delta = \frac{FL^3}{3EI}$$
;  $\theta = \frac{FL^2}{2EI}$  and  $\varepsilon \sim \frac{\delta^2}{L}$ 

#### where,

L is the length of the beams

E is the Young's modulus of the material

I is second moment of the area of the beam cross-section

#### Parallelogram flexure



$$\delta = \frac{FL^3}{24EI}$$
;  $\theta \approx 2\left(\frac{t}{b}\right)^2 \frac{\delta}{L}$  and  $\varepsilon \approx \frac{3}{5} \frac{\delta}{L}^2$ 

where

t is the thickness of the beams

b is the separation between the two beams of the parallelogram all other quantities are same as defined earlier

### Analysis contd.

#### Double Parallelogram flexure



$$\delta = \frac{FL^3}{12EI} \quad ; \quad \Theta \approx t^2 \left(\frac{1}{b_1^2} + \frac{1}{b_2^2}\right) \frac{\delta}{L} \quad \text{and} \quad \varepsilon = 0$$

Model name:ParH3DOF\_3NovDec\_LZ Study name:FEA\_nov12 Plot type : Static Deformation - Plot1 Deformation Scale 1 : 20



## Analysis contd.



#### Finite element analysis

### Planar flexures









### Micro-flexures/thermal actuators

Very Light weight = 0.07gm Integrated actuator/flexure High force



Bush et al. 03





### Micro-flexures



# Large displacement Printed flexures



Compliant Revolute joint



Compliant Prismatic joint



Compliant Universal joint



6-DOF printed Compliant parallel kinematic mechanism

### Printed flexures contd.





