

Math of fill Matrix (~~u~~)

$$\sum \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & h & h^2 & h^3 \\ 0 & 1 & 2h & 3h^2 \end{pmatrix} \begin{pmatrix} 1 \\ x \\ x^2 \\ x^3 \end{pmatrix} = P(j)$$

for coefficient  $u$

$$A_{i,i} = \int_0^h \left( \frac{d^2 \varphi(1)}{dx^2} \right)^2 dx + \int_0^h \left( \frac{d^2 \varphi(3)}{dx^2} \right)^2 dx$$

$$A_{i,i-1} = \int_0^h \varphi(1)'' \varphi(3)'' dx$$

for coefficient  $du$

$$A_{i,i} = \int_0^h (\varphi(2)'' )^2 dx + \int_0^h (\varphi(4)'' )^2 dx$$

$$A_{i,i-1} = \int_0^h \varphi(2)'' \varphi(4)'' dx$$

for coefficients involving  $u + du$

$$A_{i,i} = \int_0^h \varphi(3)'' \varphi(4)'' dx + \int_0^h \varphi(1)'' \varphi(2)'' dx$$

$$A_{i,i-1} = \int_0^h \varphi(2)'' \varphi(3)'' dx$$