

14.2)

from 6.5:  $m = -\frac{IV}{gV}$

static phase

$$mg = I \pi r^2 \frac{\partial B_z}{\partial z}$$

AC Josephson effect:

$$V = n \frac{h}{2e} f$$

where

$n = \text{some positive integer}$

dynamic phase

$$V = -\pi r^2 \dot{\nu} \frac{\partial B_z}{\partial z}$$

Quantum Hall:

$h = \text{planck's}$

$f = \text{frequency}$

$$R_H = \frac{h}{ie^2}$$

using ohm's we can swap

$$m = -\frac{IV}{gV} \Rightarrow -\frac{V^2}{R} = mgV$$

$$\frac{n^2 h^2 f^2}{4e^2} \cdot \frac{ie^2}{h} = mgV$$

$$\frac{n^2 h f^2 i}{4} = mgV$$

14.4) for a quartz resonator

$$C_c = 5 \text{ pF}$$

$$C_m = 20 \text{ fF} \quad \text{mechanical capacitance}$$

$$L_m = 3 \text{ mH} \quad \text{mechanical inductance (from inertia of crystal mass)}$$

$$R_m = 6 \text{ } \Omega$$



mechanical C + L  
are less likely to  
couple (drift thermally)

Impedances

$$Z_c = \frac{1}{i\omega C}$$

$$Z_L = i\omega L$$

$$Z_R = R$$

$$\frac{1}{Z} = \frac{1}{Z_{C_c}} + \frac{1}{Z_{C_m} + Z_{L_m} + Z_{R_m}}$$

$$\therefore Z = \left( i\omega C_c + \frac{1}{\frac{1}{i\omega C_m} + i\omega L_m + R_m} \right)^{-1}$$

See google colab for rest