# Designing with Functional Representations: GUI and Solver

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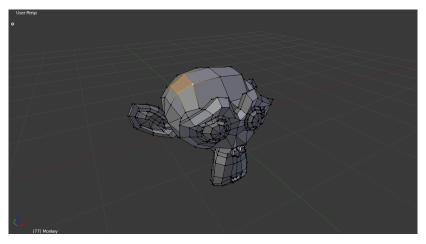
Spring 2012



### Formats for Fabrication

- How do we represent objects?
- 2D areas and 3D volumes
- Design  $\rightarrow$  fabrication

#### Data describing surface of an object



#### Advantages:

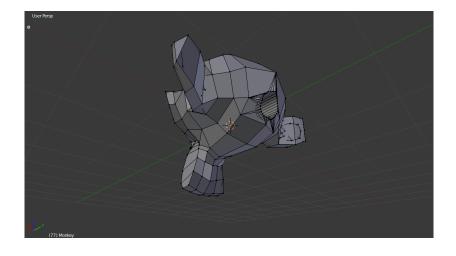
- Easy to render
- Long history
- Common in computer graphics

#### Advantages:

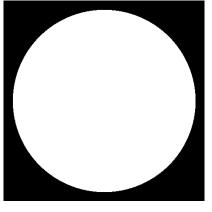
- Easy to render
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#### Disadvantages:

- Finite resolution
- Requires surface → volume conversion
- Constructive solid geometry is hard / messy

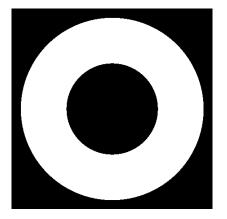


# Functional Representation



X\*X + Y\*Y < 1

# Functional Representation



(X\*X + Y\*Y < 1) && (X\*X + Y\*Y > 0.5)

# Functional Representation

- Resolution-independent
- Platform-independent
- Easy to transform and modify
- Hard to render

### Design Tools

- Library of common shapes and operators
- Python scripts as design files
- Interactive GUI:

```
cad Ul: /Users/mkeeter/grad/cba/repos/kokompe/dev/mod/test/pcb.cad
       point(J1.x-.05,J1.y+.02,z),
       point(J1.x+.05,J1.y+.02,2),
point(J1.x+.05,J1.pad[Z].y-.08,2),
       31.god[6])
005 32 = header_FTDI(')2 FTDI')
006 pcb = 32.add(pcb,x+width-.22,IC1.y-.0,z,angle=0)
ess pcb = wire(pcb,w,
       point(J2.x+.08,J2.pad[3].y,z),
783 pcb = wire(pcb,w,
784 IC1.pad[13],
       point(IC1.pod[13].x+.105,32.pod[4].y,z),
stes pcb = wire(pcb,w,
       point(IC1.pad[12].x+.07,J2.pad[5].y,z),
P313 XTAL1 = XTAL_EF08M('XTAL1\n20 MHz')
1714 pcb = XTAL1.odd(pcb,IC1.pod[4].x-.2,IC1.pod[13].y+.008,z,ongle
     IC1.pdd[2],
       point(XTAL1.x+.12,XTAL1.pod[1].v.z).
       XTAL1.pod[1])
3721 pcb = wire(pcb,w,
       point(31.pod[6].x,31.pod[6].y-.08,z),
      point(XTAL1.x-.12,XTAL1.pod[2].y,z),
```

#### Solver Fundamentals

How to convert an expression into an image?

$$(X*X + Y*Y < 1) && (X*X + Y*Y > 0.5)$$

### Solver Fundamentals

- Previous solver:
  - Brute-force evaluation
  - Paste expression into template C program
  - Compile & run!
  - Evaluates expression for every pixel

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- Previous solver:
  - Brute-force evaluation
  - Paste expression into template C program
  - Compile & run!
  - Evaluates expression for every pixel
- We can do better.

### Solver Architecture

#### Parser

- Converts string into tree structure
- Optimizes tree structure

#### Solver

- Evaluates expression on region
- Interval arithmetic speeds up evaluation
- Uses caching and multithreading

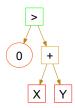
### Parser

 $\mathsf{Expressions} \to \mathsf{trees}$ 

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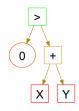
$$X + Y > 0$$
 becomes



#### Parser

Expressions  $\rightarrow$  trees

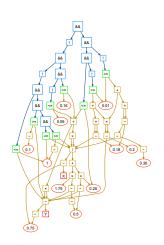
$$X + Y > 0$$
 becomes



Uses shunting-yard algorithm

#### Tree Structure

Tree of expressions operating on constants variables other expressions



#### Tree Structure

#### Distinct data types:

Floating-point value/interval Tri-bool (true, false, or ambiguous) Color (32-bit integer)



#### Architecture

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### Interval Arithmetic

■ Operations are applied to regions in space

#### Interval Arithmetic

- Operations are applied to regions in space
- Logic operations are true, false, or ambiguous
  - [-1,1] < 2 is true
  - [-1,1] < -2 is false
  - $\blacksquare$  [-1,1] < 0 is ambiguous

### Subdivision & Recursion

#### Solver algorithm:

- Evaluate on initial region
- If true or false, color and return
- If ambiguous, subdivide and recurse

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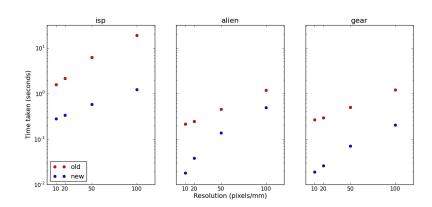
Regions below a minimum size are evaluated point-by-point, which improves performance.

# Subdivision & Recursion





### Performance



### Future Work

- Improving GUI design tools
- Generating surfaces
- Improving standard library
- Possibly switching to GPU

#### Resources



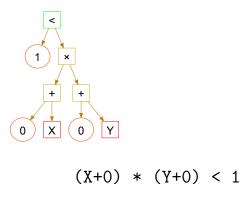
# Questions?

```
000
                                  cad UI: /Users/mkeeter/grad/cba/repos/kokompe/dev/mod/test/mbrot_color.cad
                                                                                                                                      cad ui 0.20
 1 from cad_shapes import *
  3 DEPTH = 15
  5 a = 'X'
  6 b = 'Y'
 8 mbrot = '0'
  9 for i in range(DEPTH):
        prev_level = '(pow(%s,2) + pow(%s,2)) < 4' % (a,b)
        (a, b) = ('(pow(%s,2)-pow(%s,2)+X)' % (a, b),
                  '(2*%s*%s+Y)' % (a, b))
       this_level = '(pow(\%s,2) + pow(\%s,2)) < 4' \% (a,b)
        this_level = subtract(prev_level, this_level)
        value = (int(pow(float(i+1) / DEPTH, 3) * 200.0) << 0) + 
                (int(pow(float(i+1) / DEPTH, 2) * 200.0) << 8) + \
                (int(pow(float(i+1) / DEPTH, 1) * 200.0) << 16)
        mbrot = add(mbrot, color(value, this_level))
 28 mbrot = add(mbrot, color(white, '(pow(%s,2) + pow(%s,2)) < 4' % (a,b)))
 21 # Render boundaries
 22 cad.xmin = -2
 23 cad.xmax = 0.7
 24 cad. vmin = -1.2
 25 cad.ymax = 1.2
 26 cad.mm_per_unit = 25.4 # inch units
 27 cad.type = "RGB" # Boolean or RGB
 29 cad.function = mbrot
```

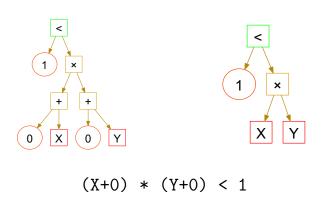
# Extra Slides

# Parser-Level Optimizations

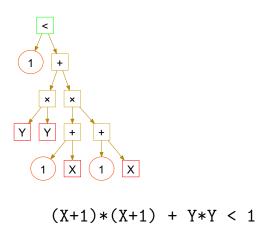
# Tree Simplification



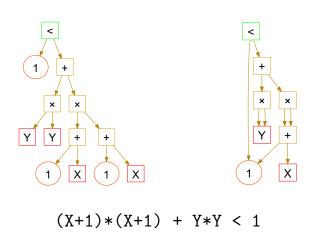
# Tree Simplification



### **Node Combination**



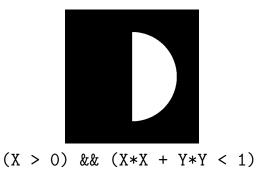
### **Node Combination**



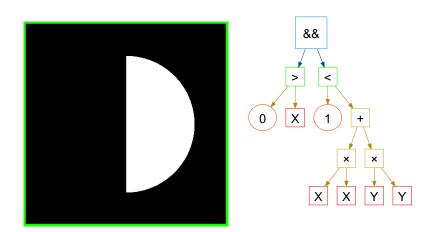
# Extra Slides

# **Solver-Level Optimizations**

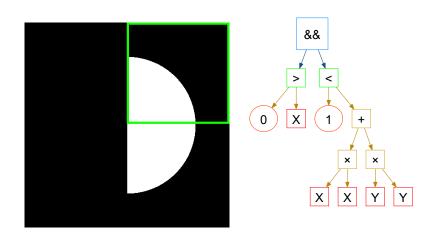
# **Branch Caching**



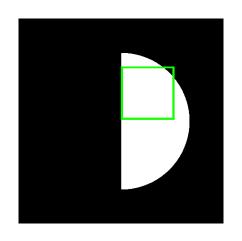
# **Branch Caching**

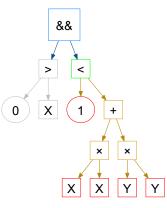


# **Branch Caching**



# **Branch Caching**



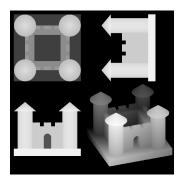


#### Multithreading

- Problem has parallel structure
- Distribute work over multiple cores:
  - Divide region evenly
  - Assign each core a subregion
- GPU could also be used

### **Z-culling**

- For 3D objects, goal is height-map
- Skip evaluation if region is occluded

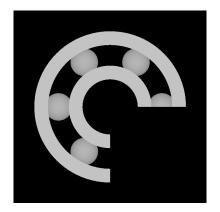


# Extra Slides

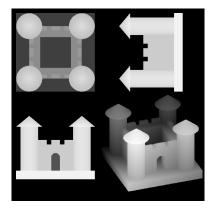
# Test Procedures & Results



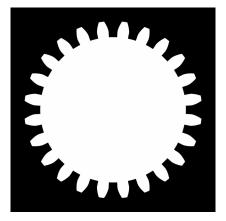
Alien



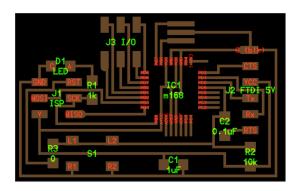
Bearing



Castle



Gear



#### File Statistics

	Dimensions			Volume	File size
File	W	Н	D	(MPixels)	(chars)
alien	3 555	3 555	1	12.6	1880
bearing	711	711	237	119.8	1 414
castle	447	447	203	40.6	49 854
gear	1 904	1 904	1	3.6	8 128
pcb	2 273	1 460	1	3.3	378 743

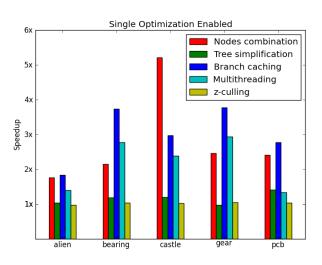
#### Speed Test Procedure

- Enable/disable one optimization (with all others optimizations disabled/enabled)
- Run 10x
- Find average run time
- Calculate speedup/slowdown

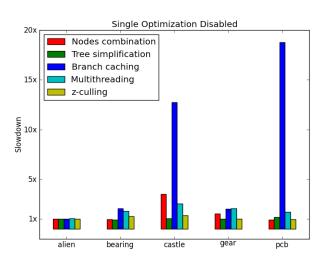
#### Caveat:

Behavior is sensitive to the selected resolution

#### Results



#### Results



Extra Slides

# Implementation & Code Details

#### Implementation Details

- 4,370 lines of C++.
- Inheritance is used for Node classes
- Parent class Node is derived into
  - NonaryNode
  - UnaryNode
  - BinaryNode

(which are further derived into operator classes)

#### **Evaluation Procedure**

- Two solve functions:
  - Float (single point)
  - Interval (region)
- Nodes store results of evaluation locally
- Nodes with children look up children's locally stored results
- Children must be evaluated before parents!

#### Tree Data Structure

- Lists of nodes, sorted by weight into levels
  - Variables and constants: weight = 0
  - Others: weight = max(child weights) + 1
- Evaluate nodes with weight = 0, then nodes with weight = 1, then nodes with weight = 2, etc.
- This order of evaluation ensures that children are evaluated before parents.

#### Branch Cache Implementation

- Each level keeps a count of "active nodes"
- "Push" (recursing on sub-interval):
  - Swap unambiguous nodes to the back of the list
  - Deactivate children of unambiguous nodes
  - Decrement active node count.
  - Save the number of cached nodes
- "Pop" (returning from recursion):
  - Increment active node count
  - Revive cached nodes
  - Activate children of revived nodes