

$$\boxed{14.1} \quad E(V) = 2E_F - 2E_C e^{-2/N_F V}$$

$$f(a) \approx \sum_{n=0}^{\infty} \frac{f^{(n)}(a)}{n!} (x-a)^n$$

$$f(0) \approx \sum_{n=0}^{\infty} \frac{f^{(n)}(0)}{n!} x^n$$

$$E^{(1)}(V) = -4E_C \frac{1}{N_F V} e^{-2/N_F V}$$

$$E^{(2)}(V) = -4E_C \frac{1}{N_F V^2} e^{-2/N_F V} \left(\frac{2}{N_F V} - 1 \right)$$

$$E^{(3)}(V) = -8E_C \frac{1}{N_F V^3} e^{-2/N_F V} \left(1 - \frac{4}{N_F V} + \frac{2}{N_F^2 V^2} \right)$$

} $E^{(n)}(0)$ undefined if

?

Try again:

$$e^x \text{ st. } x=0 \approx \sum_{n=0}^{\infty} \frac{x^n}{n!}$$

$$e^{-2/N_F V} \approx \sum_{n=0}^{\infty} \frac{\left(\frac{-2}{N_F V}\right)^n}{n!}$$

$$E(V) \approx 2E_F - 2E_C \sum_{n=0}^{\infty} \frac{1}{n!} \left(\frac{-2}{N_F V}\right)^n$$

14.2

$$V = n \frac{h}{2e} f$$

$$R_H = \frac{1}{n} \frac{h}{e^2}$$

$$\hookrightarrow V = IR_H$$

$$\hookrightarrow I = \frac{V}{R_H} = \frac{n \frac{h}{2e} f}{\frac{1}{n} \frac{h}{e^2}} = \frac{1}{2} n^2 f e$$

$$IV = mgv$$

$$\hookrightarrow \frac{1}{2} n^2 f e \cdot n \frac{h}{2e} f = mgv$$

$$\boxed{\frac{1}{4} n^3 f^2 h = mgv}$$

$$\boxed{14.3} \quad \Phi_0 = 2.07 \times 10^{-7} \text{ G} \cdot \text{cm}^2$$

$$1 \text{ cm}^2 = \pi r_{\text{squid}}^2$$

$$\hookrightarrow r_{\text{squid}} = .56 \text{ cm} = .0056 \text{ m}$$

Magnetic field of a current-carrying wire:

$$\text{Ampere's law: } \oint \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{enclosed}}$$

$$B \cdot 2\pi r = \mu_0 I$$

$$B = \frac{\mu_0 I}{2\pi r}$$

$$(x - x_0)^2 + y^2 = r^2$$

$$y = \pm \sqrt{r^2 - (x - x_0)^2}$$

$$B(x) = \frac{\mu_0 I}{2\pi x}$$

$$\Phi = \iint_A B(x) dA$$

$$= \int_{x_0-r}^{x_0+r} \frac{\mu_0 I}{2\pi x} \int_{-\sqrt{r^2-(x-x_0)^2}}^{+\sqrt{r^2-(x-x_0)^2}} dy dx$$

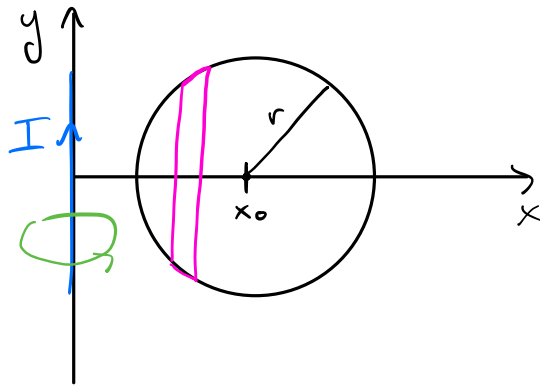
$$= \int_{x_0-r}^{x_0+r} \frac{\mu_0 I}{2\pi x} \cdot 2\sqrt{r^2-(x-x_0)^2} dx$$

$$= \frac{\mu_0 I}{\pi} \int_{x_0-r}^{x_0+r} \frac{\sqrt{r^2-(x-x_0)^2}}{x} dx$$

$$= \frac{\mu_0 I}{\pi} \sqrt{r^2 - x_0^2} \left[\ln(r^2 - rx_0) - \ln(-r^2 + rx_0) \right] + \pi x_0$$

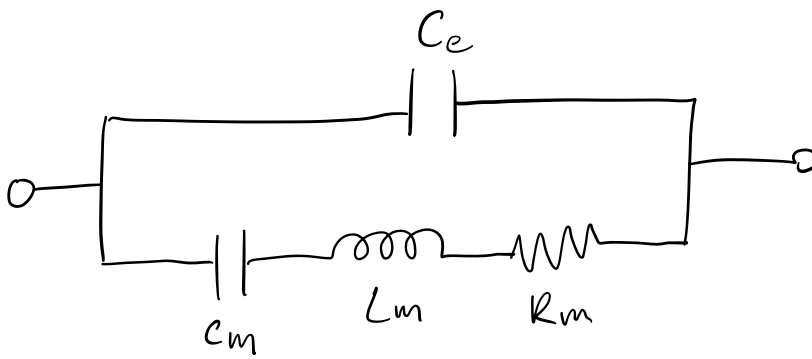


$$\ln\left(\frac{r^2 - rx_0}{-(r^2 - rx_0)}\right) = \ln(-1) ?$$



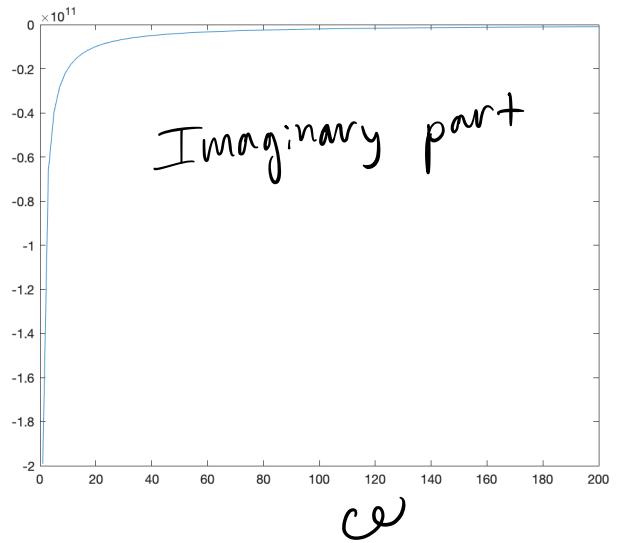
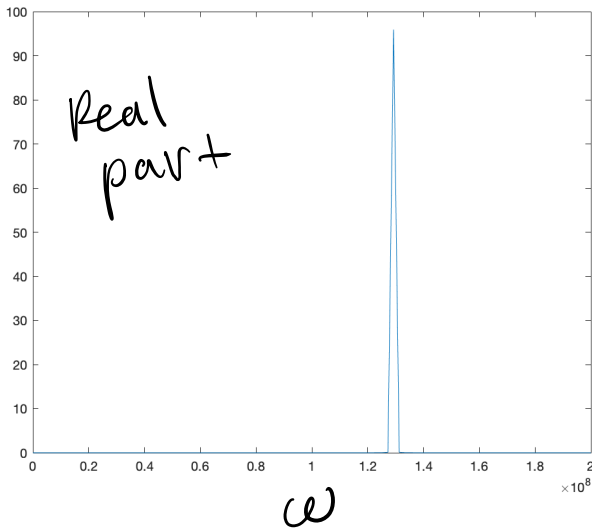
Solve $\Phi(x_0) = \Phi_0$ for $I = 1 \text{ A}$ and $r = .0056 \text{ m}$

14.4

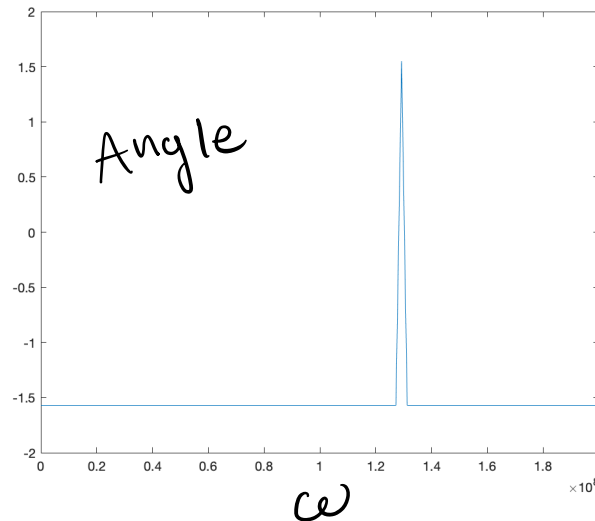


$$Z = \frac{1}{j\omega C_e} \parallel \left(\frac{1}{j\omega C_m} + j\omega L_m + R_m \right)$$

$$Z = \frac{1}{j\omega C_e + \frac{1}{\left(\frac{1}{j\omega C_m} + j\omega L_m + R_m \right)}}$$



Resonance =
 $\frac{1}{\sqrt{L_m C_m}} = 1.3 \times 10^8 \frac{\text{rad}}{\text{s}}$
 Smaller capacitance dominates



14.5

Harrison chronometer: 1 s/day accuracy

Based on earth circumference = 21641 n.m.

↳ $1^\circ = 60$ n.m.

Earth revolves @ $360^\circ / 24$ hrs $\rightarrow 1^\circ = 4$ min

$\therefore 4$ min error = 60 n.m. $\rightarrow 1$ min error = 15 n.m.

$\therefore 1$ month = 30.44 days $\rightarrow 30.44$ s error = 0.507 min error

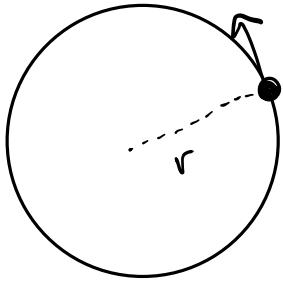
$\rightarrow 7.61$ n.m. error

Atomic clock: 10^{-12} s/s = 8.64×10^{-8} s error per day

1 month = 30.44 days $\rightarrow 2.63 \times 10^{-6}$ s error = 4.38×10^{-8} min error

$\rightarrow 6.58 \times 10^{-7}$ n.m. error

14.6



$$r = 2.018 \times 10^7 \text{ m} + 6.38 \times 10^6 \text{ m} = 2.66 \times 10^7 \text{ m}$$

$$a) \quad a = \frac{v^2}{r} = \frac{GM}{r^2}$$

$$\hookrightarrow v = \sqrt{\frac{GM}{r}} = \boxed{3871 \text{ m/s}}$$

$$b) \quad 2\pi \cdot 2.66 \times 10^7 \text{ m} = v \cdot T$$

$$T = 43175 \text{ s} = \boxed{12 \text{ hours}}$$

c) ?

d) Slower on earth

$$\frac{t_{\text{earth}}}{t_{\text{sat}}} = \frac{1 - \frac{GM}{6.38 \times 10^6 \text{ m} \cdot c^2}}{1 - \frac{GM}{2.66 \times 10^7 \text{ m} \cdot c^2}} = .99999999947158$$

2.26×10^{-5} s error per 12 hrs