

In[118]:=

ClearAll[QFn, k, m, ω, γ]

(*calculating q based on ω₀ / width at .5 max val*)

In[99]:= **ω₀ = Sqrt[k / m]**

Out[99]= $\sqrt{\frac{k}{m}}$

In[119]:= **QFn = 2 γ² (k / m) == (k - m ω²)² + (γ ω)²**

ws = Solve[QFn, ω]

ω₋ = ω /. ws[[2]]

ω₊ = ω /. ws[[4]]

Q = ω₀ / (ω₊ - ω₋)

Out[119]= $\frac{2 k \gamma^2}{m} == \gamma^2 \omega^2 + (k - m \omega^2)^2$

Out[120]= $\left\{ \left\{ \omega \rightarrow -\frac{\sqrt{\frac{2 k}{m} - \frac{\gamma^2}{m^2} - \frac{\gamma \sqrt{4 k m + \gamma^2}}{m^2}}}{\sqrt{2}} \right\}, \left\{ \omega \rightarrow \frac{\sqrt{\frac{2 k}{m} - \frac{\gamma^2}{m^2} - \frac{\gamma \sqrt{4 k m + \gamma^2}}{m^2}}}{\sqrt{2}} \right\}, \right.$

$\left. \left\{ \omega \rightarrow -\sqrt{\frac{k}{m} - \frac{\gamma^2}{2 m^2} + \frac{\gamma \sqrt{4 k m + \gamma^2}}{2 m^2}} \right\}, \left\{ \omega \rightarrow \sqrt{\frac{k}{m} - \frac{\gamma^2}{2 m^2} + \frac{\gamma \sqrt{4 k m + \gamma^2}}{2 m^2}} \right\} \right\}$

Out[121]= $\frac{\sqrt{\frac{2 k}{m} - \frac{\gamma^2}{m^2} - \frac{\gamma \sqrt{4 k m + \gamma^2}}{m^2}}}{\sqrt{2}}$

Out[122]= $\sqrt{\frac{k}{m} - \frac{\gamma^2}{2 m^2} + \frac{\gamma \sqrt{4 k m + \gamma^2}}{2 m^2}}$

Out[123]= $\frac{\sqrt{\frac{k}{m}}}{-\frac{\sqrt{\frac{2 k}{m} - \frac{\gamma^2}{m^2} - \frac{\gamma \sqrt{4 k m + \gamma^2}}{m^2}}}{\sqrt{2}} + \sqrt{\frac{k}{m} - \frac{\gamma^2}{2 m^2} + \frac{\gamma \sqrt{4 k m + \gamma^2}}{2 m^2}}}$

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In[117]:= (*m = k = 1  
          γ = .1  
          ω+  
          ω-  
          Q*)
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(*calculating Q for an undamped oscillator *)
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